

Chemistry 342  
Spring, 2001  
Problem Set 1

Due Wednesday, August 29

Read pages 14-30 in Atkins. Do the following Problems in Chapter 1: 1, 2, 3, 4, 7, 10, 13, 14. Also, answer the following question:

The Maxwell-Boltzmann velocity distribution function that we learned about in class refers to the number density of particles, i.e., the number of particles per unit volume having a speed between  $v$  and  $v+dv$ :  $\frac{n(v)dv}{n_0} = \frac{4n_0}{\sqrt{\pi}} \frac{v^2}{\alpha^2} e^{-v^2/\alpha^2} dv / \alpha$ , where  $n_0$  is the number density of particles and  $\frac{1}{2}m\alpha^2 = kT$ . Note that the speed can have values  $0 \leq v \leq \infty$ .

Another important distribution function is the flux density of particles (number of particles striking a target area per unit time), which is given by

$\frac{n_f(v)dv}{n_{f,0}} = C \frac{v^3}{\alpha^3} e^{-v^2/\alpha^2} dv / \alpha$ , where  $C$  is a normalization constant, and  $n_{f,0}$  is the total flux of particles.

- Evaluate the constant,  $C$ .
- Determine the average speed for this distribution function.
- Determine the most probable speed for this distribution function.
- Determine the root mean square speed for this distribution function.

Express your answers to parts B-D as multiples of  $\alpha$ .

Some useful integrals:

$$\int_0^{\infty} x^{2n} e^{-ax^2} dx = \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{2^{n+1} a^n} \sqrt{\frac{\pi}{a}}$$

$$\int_0^{\infty} x^{2n+1} e^{-ax^2} dx = \frac{n!}{2a^{n+1}}$$